

# LCLS S-band Structure Coupler

Zenghai Li

*Advanced Computations Department*

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# Outline



- 
- Motivation
  - Modeling tool
  - S3P model of S-band coupler
  - Field analysis
  - Beam analysis

## Discussions

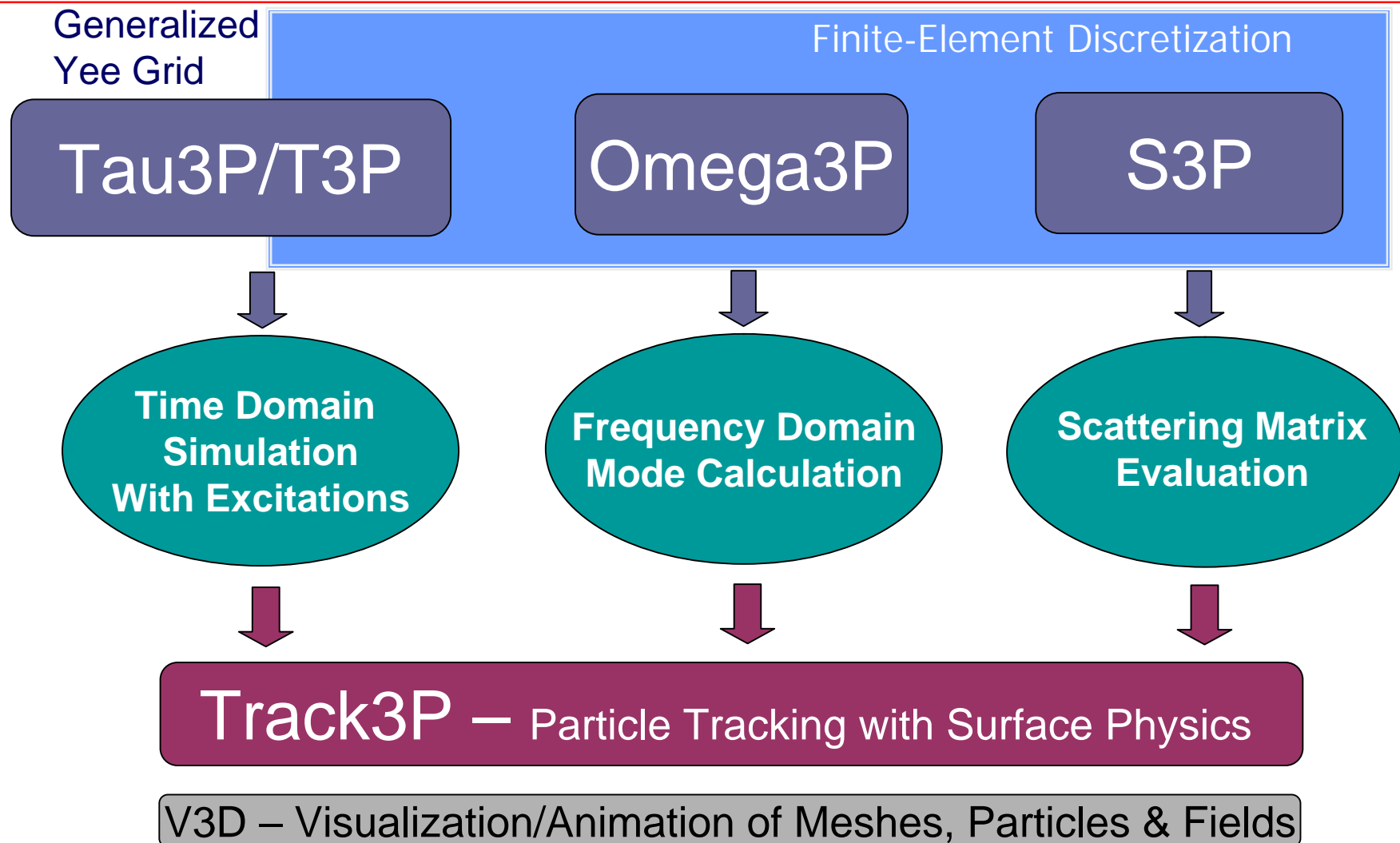
# Motivation

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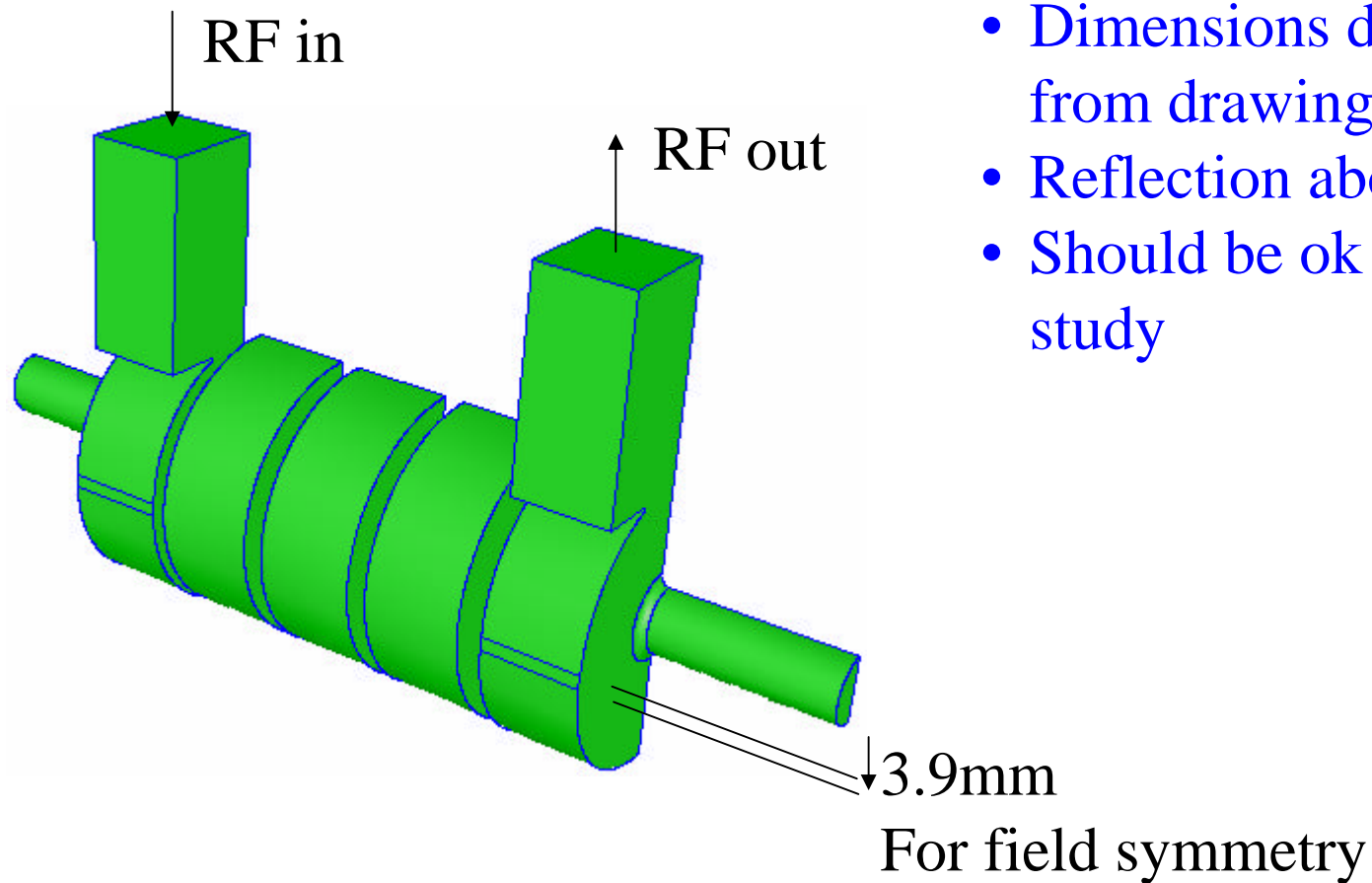


- To understand effects of multipole fields on beam dynamics in single-feed coupler
- Work on alternative designs if necessary

# Parallel EM Codes On Unstructured Grids

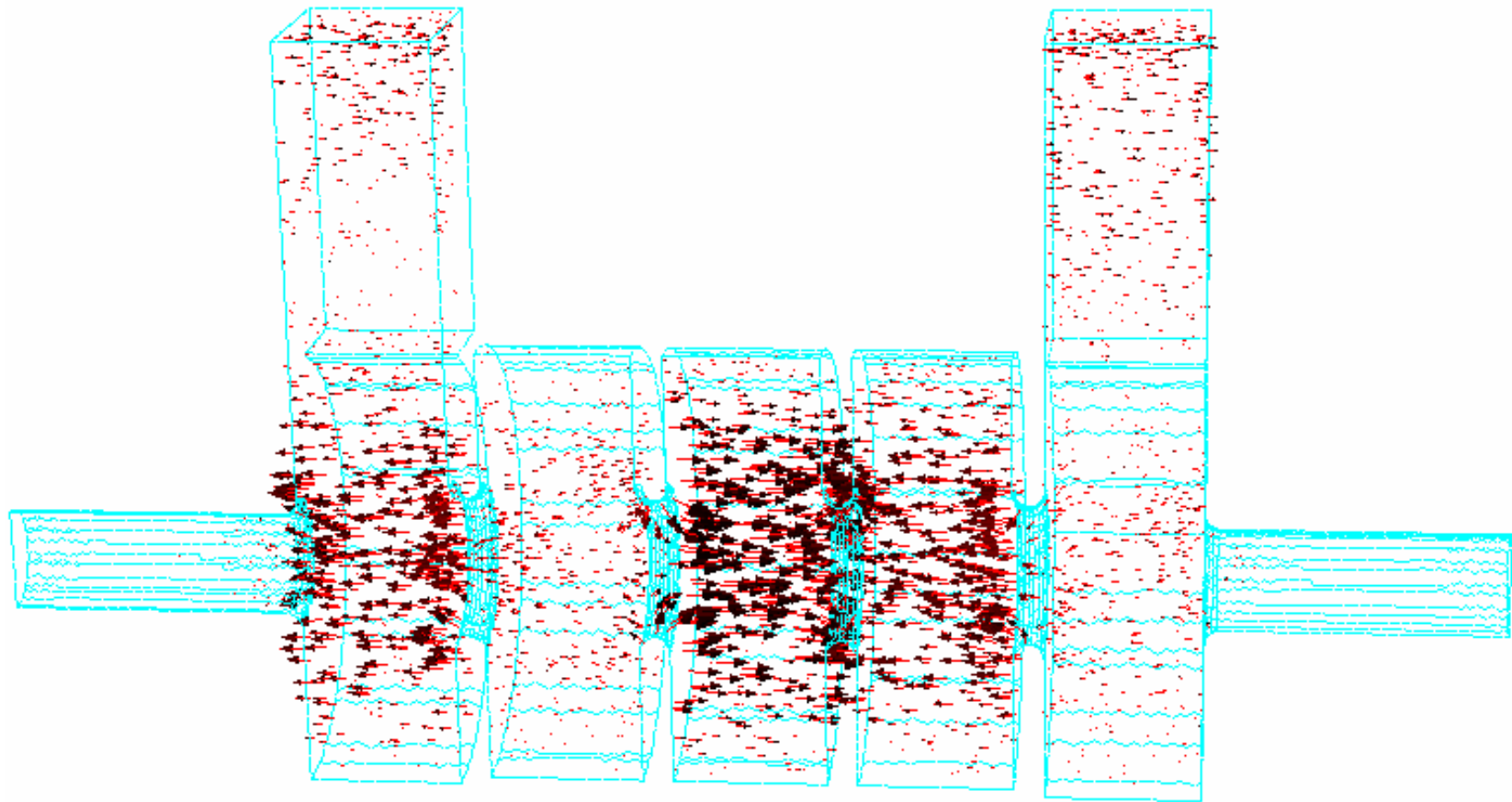


# LCLS S-Band Coupler – S3P Model

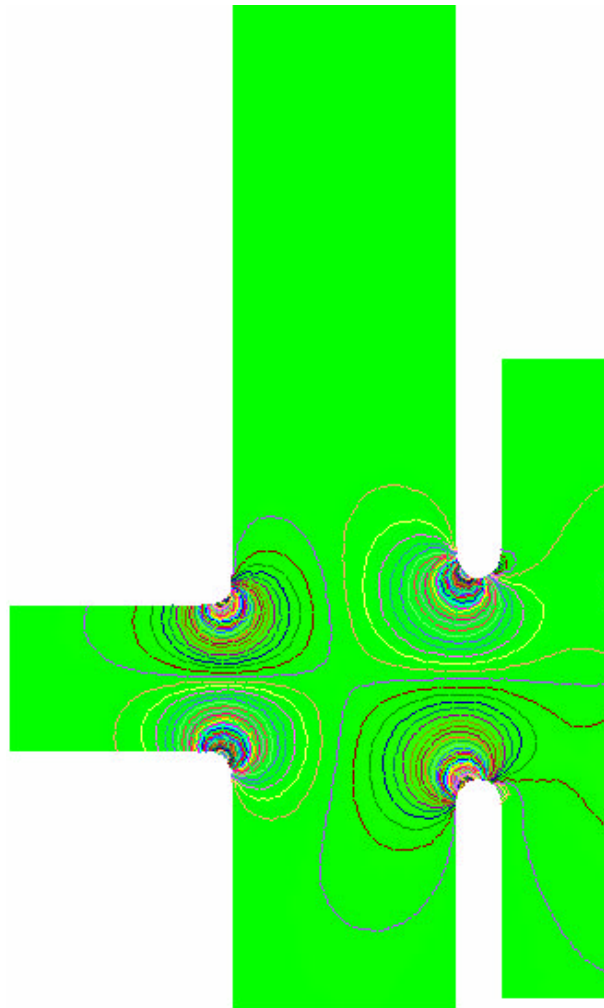


- Dimensions directly from drawings
- Reflection about 0.05
- Should be ok for this study

# Field Snapshot



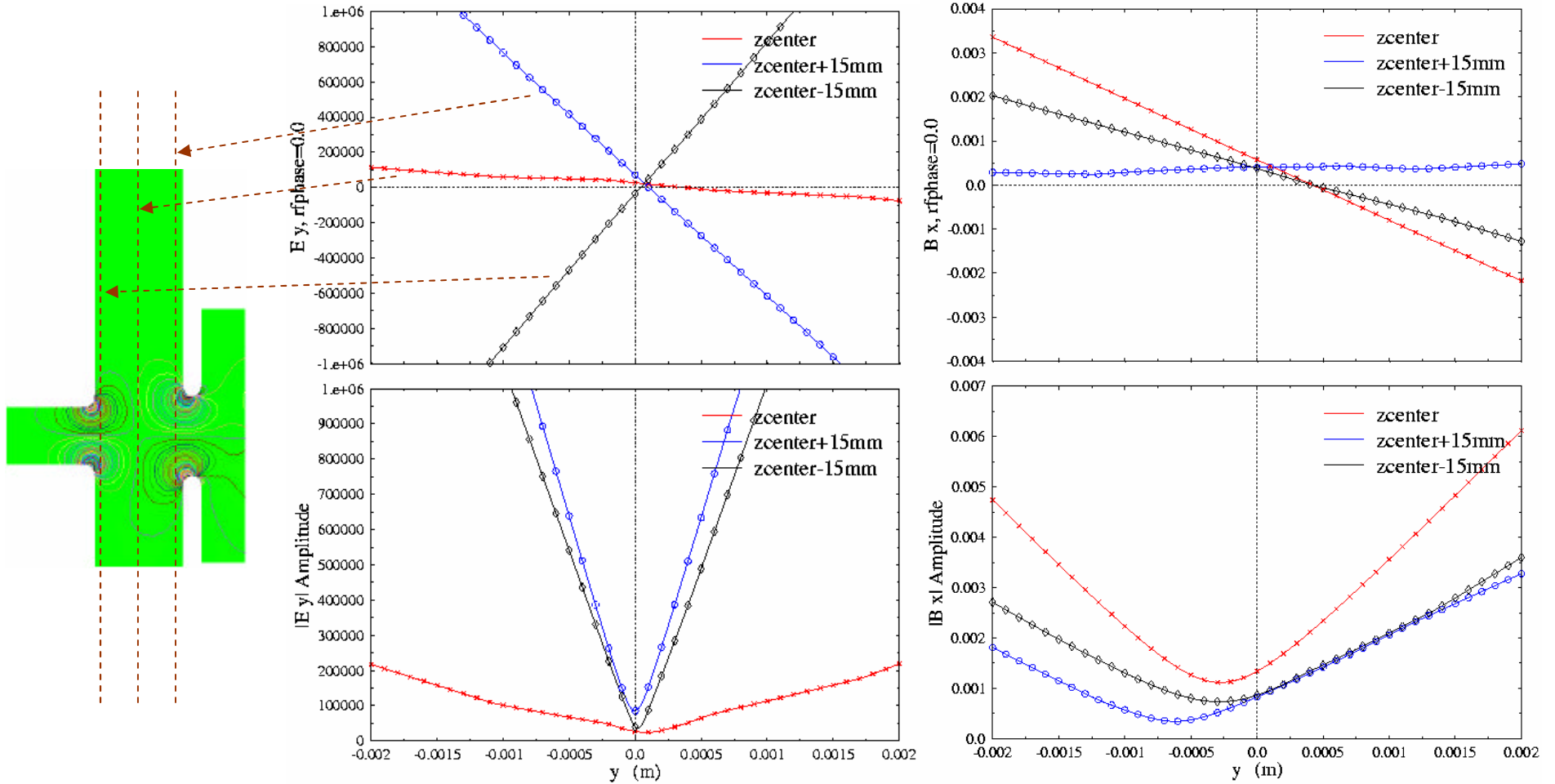
# Field Asymmetry In Coupler Cell - Ey



$E_y$ :

- Snapshot
- Contour plot

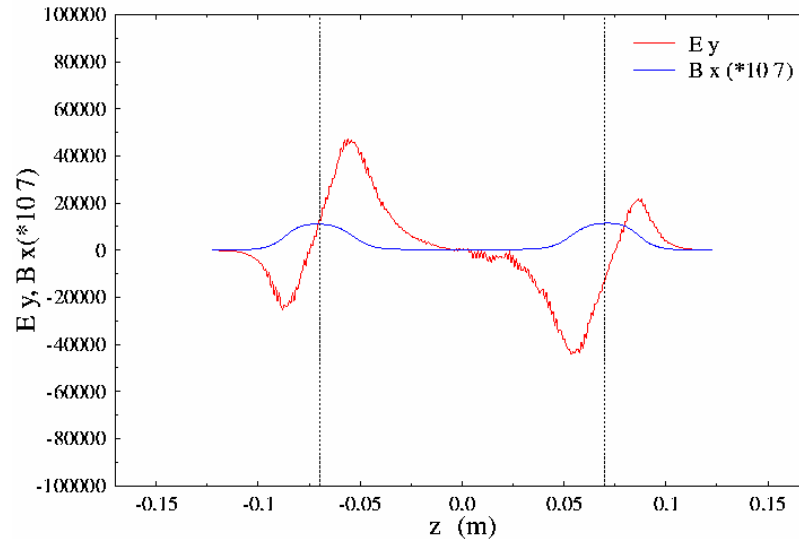
# Field Asymmetry





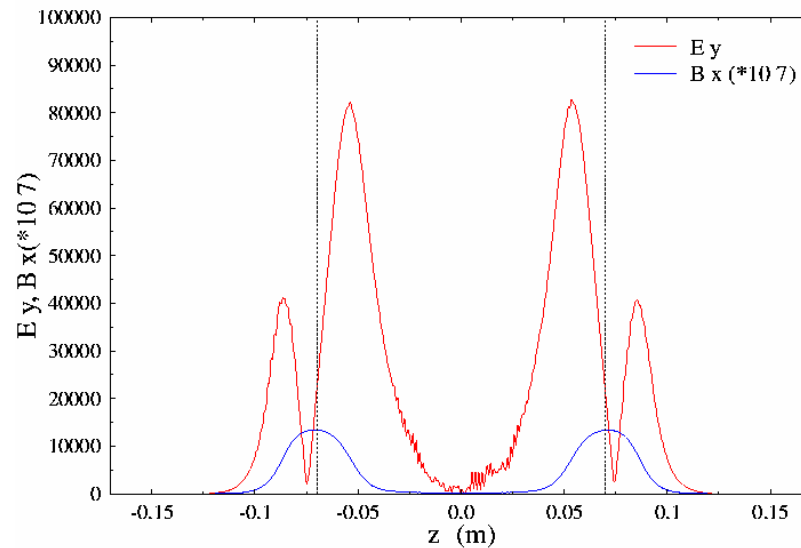
# Fields On Axis

E and B on axis, t=0.0



On-axis  $E_y$  and  $B_x$  are non-zero in the coupler region

E and B on axis, Amplitude



# Beam Dynamics

- Equation of motion:  $\frac{d(\mathbf{g}\bar{\mathbf{b}})}{dt} = \frac{e}{m_0 c} (\bar{\mathbf{E}} + c\bar{\mathbf{b}} \times \bar{\mathbf{B}})$
- Transverse momentum

$$\Delta\bar{\mathbf{P}}_{m\perp} = -\frac{je}{\mathbf{w}} \nabla_{\perp} \int E_z(r, \mathbf{q}, z, m) e^{j\omega t - jz_z z} dz dz$$

$$E_z(r, \mathbf{q}, z, z_z) = \sum_{m=0}^{\infty} A_m J_m(\mathbf{h}_r r) \cos(m\mathbf{q}) e^{-jz_z z} + \sum_{m=0}^{\infty} B_m J_m(\mathbf{h}_r r) \sin(m\mathbf{q}) e^{-jz_z z}$$

$$\text{where } \mathbf{h}_r^2 + \mathbf{z}_z^2 = \frac{\mathbf{w}^2}{c^2}$$

- To the first order

$$\Delta\bar{\mathbf{P}}_{\perp} = -\frac{je}{\mathbf{w}} \left( \underbrace{-\frac{\mathbf{h}_r^2 A_0}{2} (x\hat{x}_0 + y\hat{y}_0)}_{\text{focusing}} + \underbrace{\frac{\mathbf{h}_r A_1}{2} \hat{x}_0 + \frac{\mathbf{h}_r B_1}{2} \hat{y}_0}_{\text{dipole}} + \underbrace{\frac{\mathbf{h}_r^2 A_2}{4} (x\hat{x}_0 - y\hat{y}_0)}_{\text{quad}} + \underbrace{\frac{\mathbf{h}_r^2 B_2}{4} (y\hat{x}_0 + x\hat{y}_0)}_{\text{skew quad}} \right)$$

# $\gamma$ Dependence Of Momentum Multipoles



- $1/\gamma$  dependence for azimuthal focusing (full structure - back-back coupler in our case)

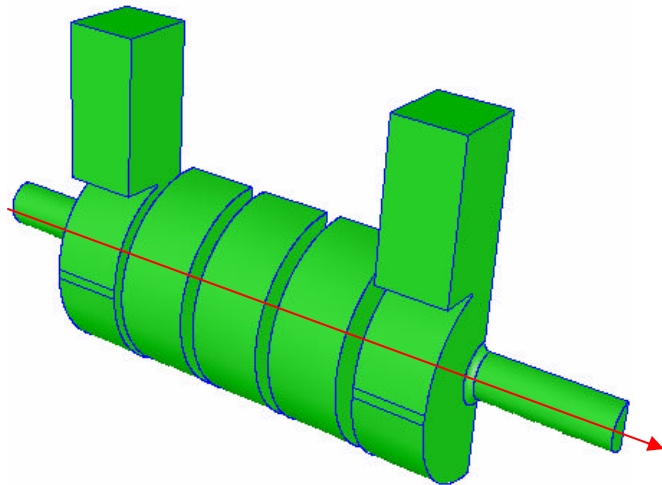
$$\mathbf{g}(\infty)\mathbf{b}_r(\infty) = \mathbf{g}(-\infty)\mathbf{b}_r(-\infty) \overbrace{\left(1 + \frac{I_{01}}{\mathbf{g}} + \frac{I_{02} - I_{03}}{\mathbf{g}^2}\right)}^{\text{Adiabatic damping}} - r(a) \overbrace{\left(\frac{I_{11}}{\mathbf{g}} + \frac{I_{12} - I_{13} + I_{14}}{\mathbf{g}^2}\right)}^{\text{RF focusing}}$$

where  $I_{mn}$  are integrals of  $E_z$  field

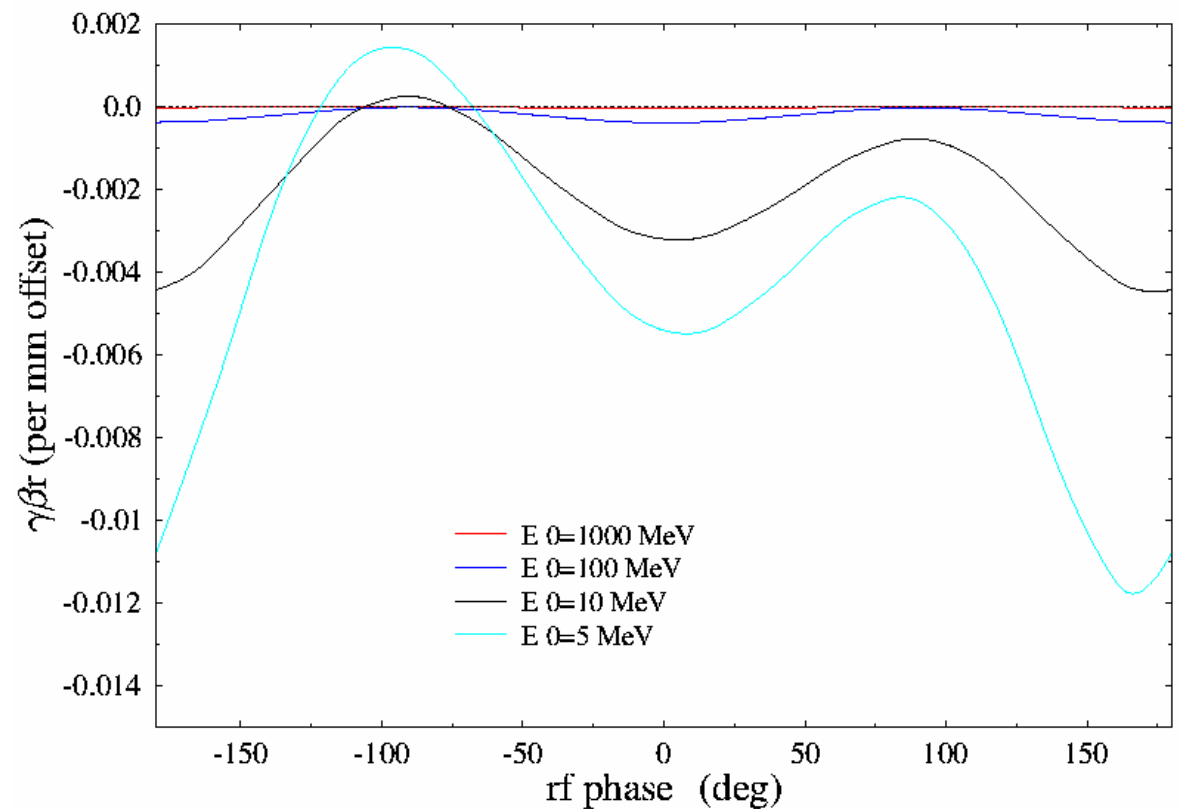
- Dipole and quadrupole are  $\gamma$  independent.

# Azimuthal Focusing

- Full back-back system simulation



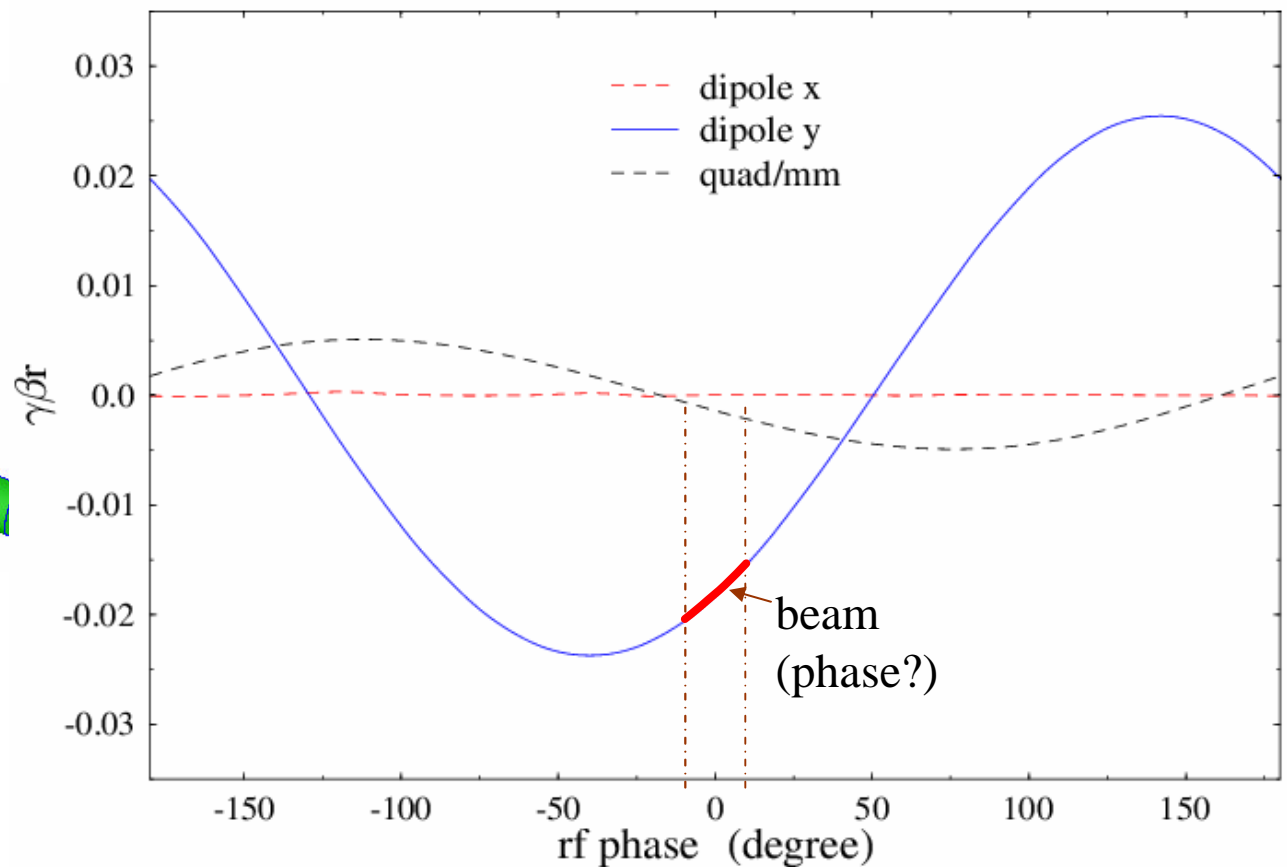
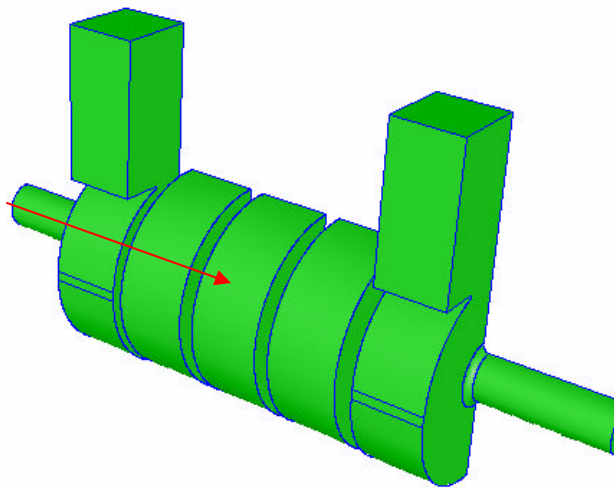
Azimuthal Focusing v.s. Initial Energy



# Dipole & Quadrupole

- Effect of input coupler
- Integrate through half of the model

Dipole & Quadrupole v.s. RF Phase



# Head-Tail Effect

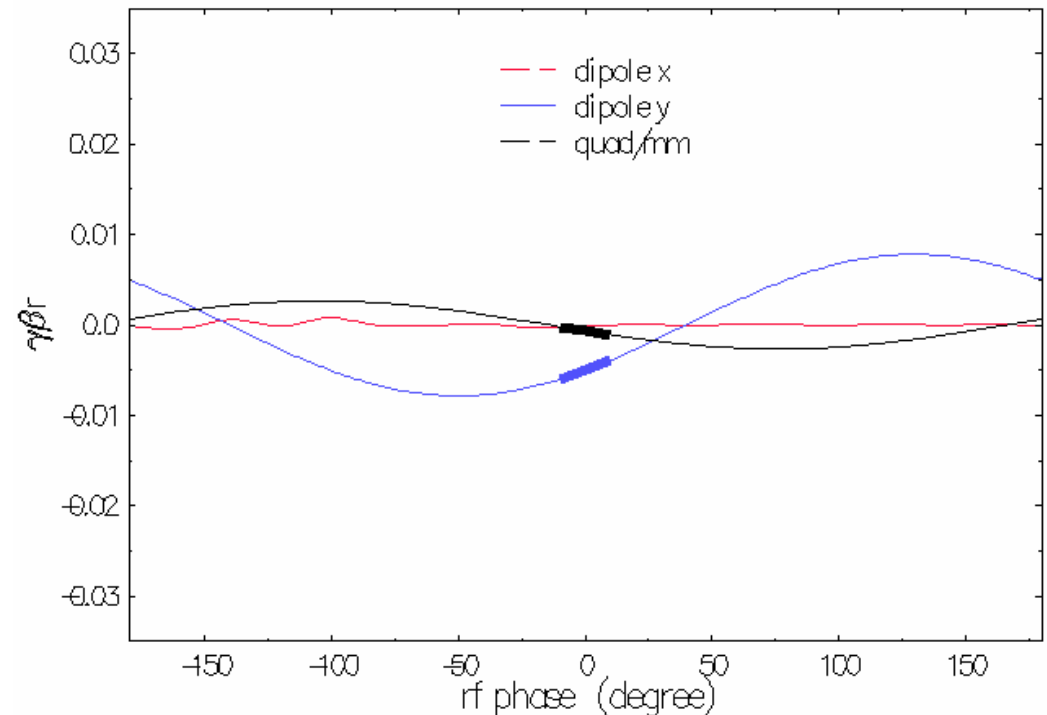
- “Zero” phase is not accurate since only a few cells are included in the present model – phase slippage and coupler effect significant
- Amplitude of dipole and quadrupole OK
- Bunch spans  $\pm 10$  degrees in RF phase
- If beam on crest, head to tail  $\Delta(\gamma\beta_{\perp})$  is
  - Dipole  $\Delta(\gamma\beta_{\perp}) : 0.005$
  - Quadrupole  $\Delta(\gamma\beta_{\perp}) : 0.0015/\text{mm}$  (focusing)

# Output Coupler

Iris dimension adjusted to obtain a good match

- Adjust amount: 0.75mm
- Tuned in real structure

Output: Dipole & Quadrupole v.s. RF Phase



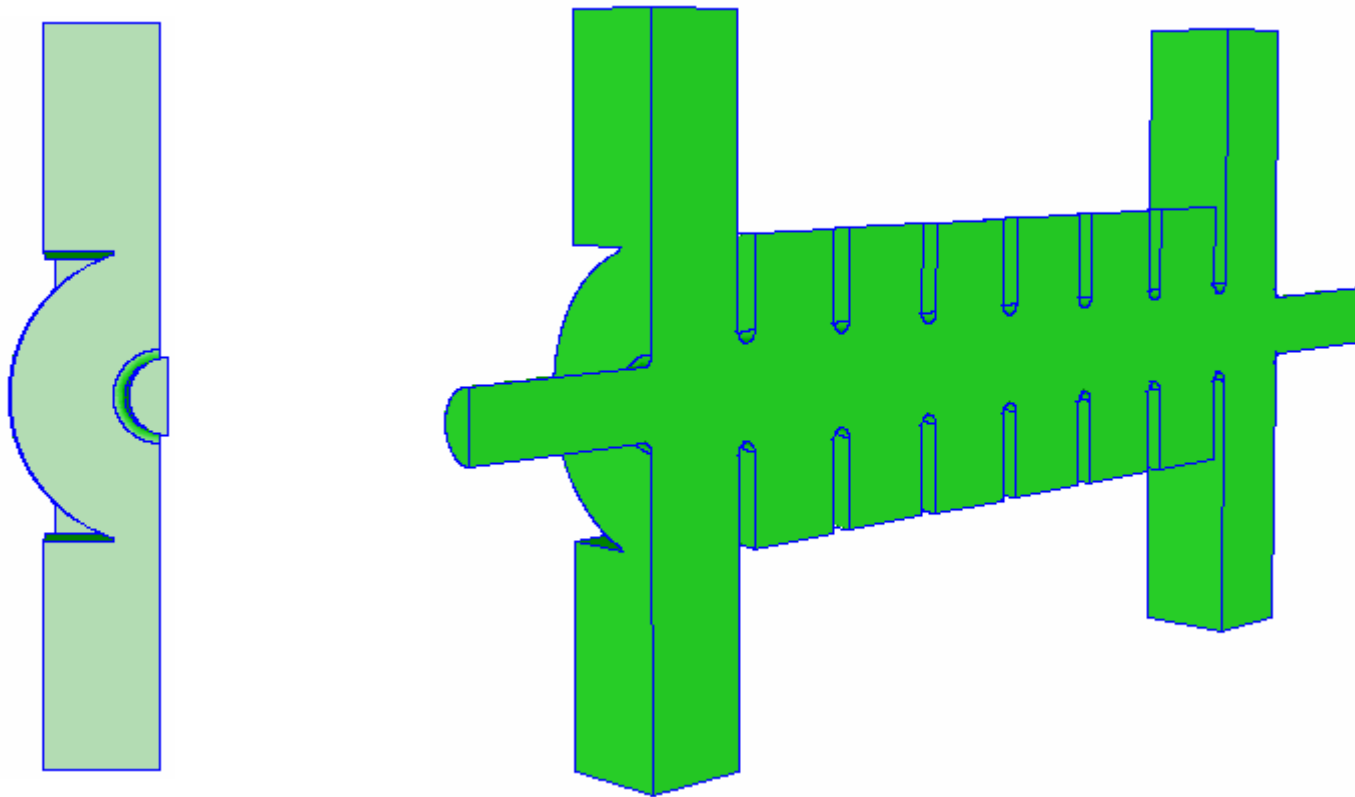
$$\gamma \approx 100$$

$\pm 10$  degree bunch length

Dipole  $\Delta(\gamma\beta_{\perp}) : 0.0021$

Quadrupole  $\Delta(\gamma\beta_{\perp}) : 0.00088/\text{mm}$  (focusing)

# Input Coupler – Duel-feed

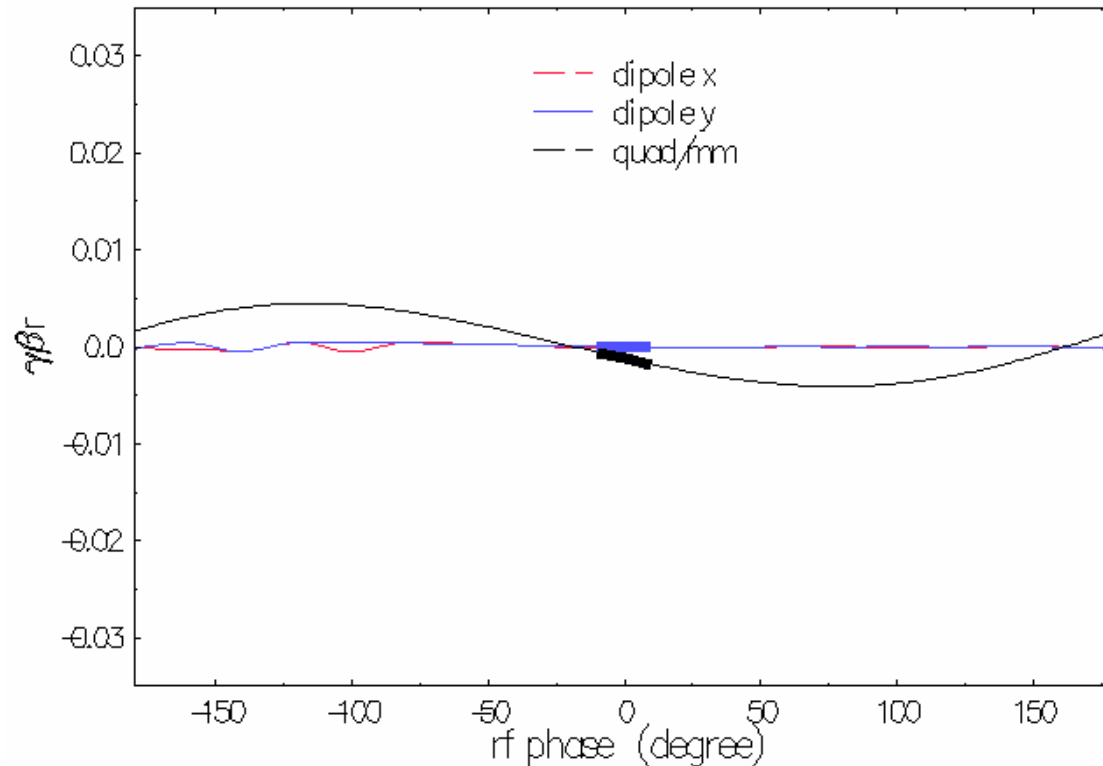


Width change: 3.502 mm  
Cell radius change: 0.800 mm  
Iris thickness unchanged



# Input Coupler – Duel-feed

Input Duel: Dipole & Quadrupole v.s. RF Phase

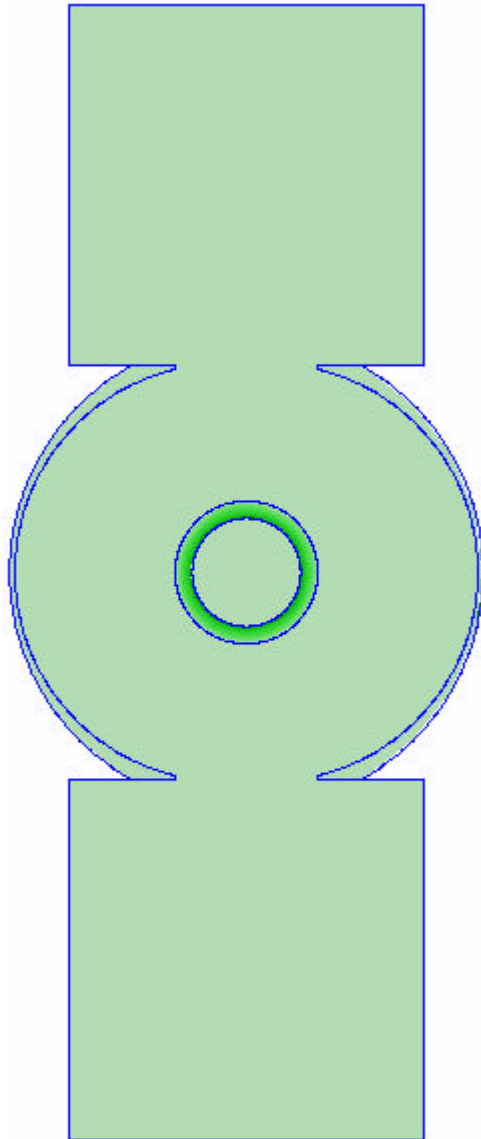


$\gamma \approx 10$

$\pm 10$  degree bunch length

Quadrupole  $\Delta(\gamma\beta_{\perp})$  : 0.00125/mm (focusing)

# Input – Racetrack Duel-feed



Need to

- Match
- Check quad

# Cecile's Quad Requirement

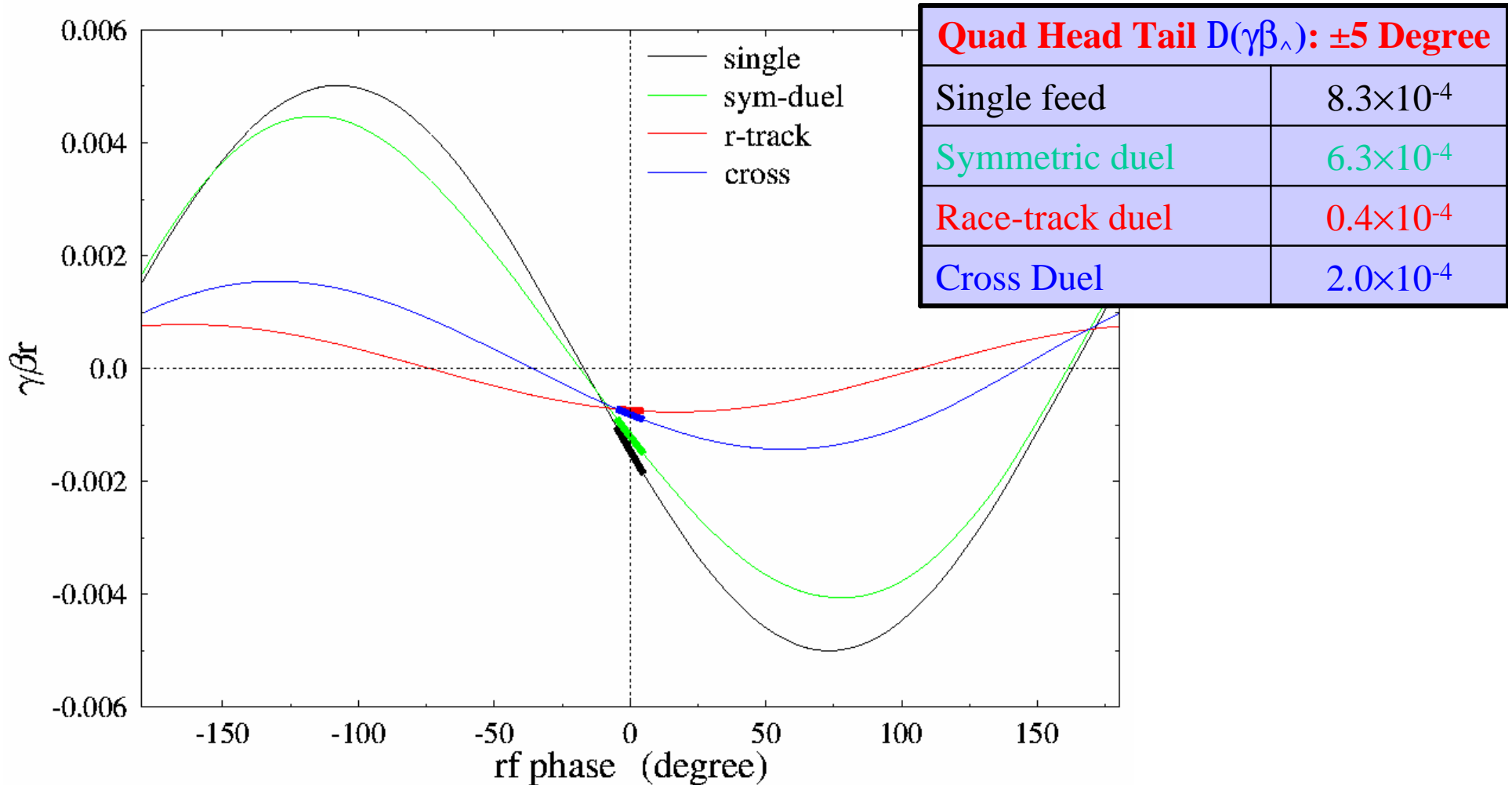
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- Head-tail angle:  $0.075\text{rad/m}$
- Input dual-feed, cylindrical cell:  $0.0625\text{rad/m}$
- Output single-feed:  $0.0044\text{rad/m}$  (OK)

( $\gamma$  is a factor of 10 large at output)

# Coupler Comparison

## S-band Input Coupler: Quadrupole v.s. RF Phase



# Race-track & Cross Coupler

